

# Speed Control for Direct Torque Control Permanent Magnet Synchronous Motor

Dr. Abbas H. Abbas\*, Dr. Alaa A. Hassan\*\*, Dhiaa K. Shary\*\*

\*Electrical Engineering Department- College of Engineering -University of Basrah, Basrah-Iraq

\*\*Electrical Engineering Department-Technical College of Basrah-Foundation of Technical Education, Basrah-Iraq

**Abstract**—In this paper, the modeling of the Direct Torque Control (DTC) system of permanent magnet synchronous motor (PMSM) based on Matlab/Simulink environment is presented. Simulation results are introduced to predict the motor drive system performance and the effect of PI controller parameters on speed response in this system. The simulation also shows the torque ripple can be reduced by narrowing the torque hysteresis loops width.

**Index terms**—Permanent synchronous motor (PMSM), direct torque control (DTC), PI control.

## I. INTRODUCTION

Direct Torque Control (DTC) is a popular control technique widely applied in motor drive applications since it was proposed by Depenbrock and Takahashi [1, 2]. By directly controlling the flux and torque, both techniques yield fast dynamic response and high performance [3].

The basic principle of DTC is to directly select stator voltage vectors according to the differences between the references and actual torque and stator flux linkage [4].

The DTC has many favorable features, such as no need of complicated coordinate transformation and pulse width modulation (PWM). Also, it is insensitive to motor parameters, which is inevitable in the vector control scheme. A major problem associated with the popular DTC is the big torque and flux ripples because of the use of two simple two-value hysteresis controllers for the stator flux linkage and the torque. In addition, the use of a  $60^\circ$  angular region based signal for choosing the space voltage vector applied to the stator windings, which is so crude that none of these space voltage vectors generated by the voltage source inverter (VSI) could offer a precise control of the torque and the stator flux linkage at the same time. These ripples can be reduced if the errors of the torque and the flux linkage, and the angular position signal of the flux linkage are subdivided into several smaller subsections. By choosing a more accurate space voltage vector, more accurate control of torque and flux linkage can be obtained [5].

Management is a structured process that aims to Managing risk is to identify an event that hurt the company in the future. This includes taking action to avoid or reduce the things that are not desirable company. This is what lies behind the need did a study to determine any potential hazards in the system and calculate the value of the risk in order to analyze and avoid risks that could hurt the company.

In this paper, the DTC of PMSM is proposed and the choice of null-vectors and vector sequence are properly selected to improve the performance of motor drive system.

## II. THE MATHEMATIC MODEL OF PMSM

The model of the PMSM is derived by using d and q variables in a rotor reference frame, the voltage equations are:

$$V_d = R_s i_d + d\Phi_d/dt - \omega \Phi_q \quad (1)$$

$$V_q = R_s i_q + d\Phi_q/dt + \omega \Phi_d + \omega \Phi_f \quad (2)$$

It is noted that the stator flux linkage components are:

$$\Phi_d = L_d i_d + \Phi_f \quad (3)$$

$$\Phi_q = L_q i_q \quad (4)$$

Where  $R_s$  is the stator winding resistance,  $L_d$  and  $L_q$  are d-q axis inductances,  $\Phi_f$  is the rotor flux linkage generated by the permanent magnets,  $V_d$  and  $V_q$  are the d-q axis voltages,  $\Phi_d$  and  $\Phi_q$  are d-q axis fluxes,  $i_d$  and  $i_q$  are d-q axis currents and  $\omega$  is the angular speed of the rotor [6, 7].

The mechanical torque equation referred to motor-load system is given by:

$$T_e = (J/P) dw/dt + (D/P) W + T_L \quad (5)$$

with

$$T_e = \frac{3}{2} p (\Phi_d i_d + (L_d - L_q) i_d i_q) \quad (6)$$

where  $D$  is the damping torque coefficient,  $J$  is the moment of inertia of rotor,  $T_L$  is the load torque and  $P$  is the number of pole pairs [8, 9].

## III. DIRECT TORQUE CONTROL STRATEGY

### A- Control of stator flux linkages

When the motor is fed from a three-phase inverter, the stator voltage is determined by the status of the power switches. Therefore, there are six non-zero voltage vectors,  $V_1(100)$ ,  $V_2(110)$ , ..., and  $V_6(101)$ , and two zero voltage vectors,  $V_7(000)$  and  $V_8(111)$ . Two zero voltage vectors are at the origin and the six non-zero vectors are  $60^\circ$  apart from each other in voltage vector plane as in Fig.(1). Both the amplitude and rotating speed of the stator flux linkage can be controlled by selecting the proper stator voltage vectors [10].

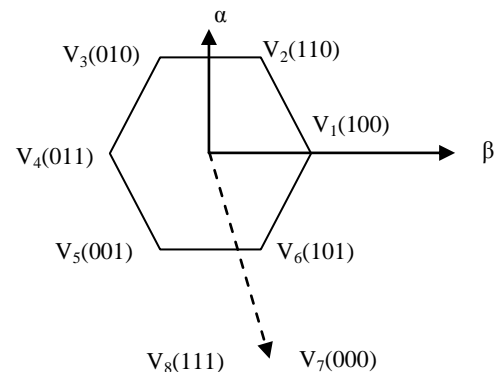


Fig. 1. Sectors of stator flux linkage.

**B- Control of the amplitude of stator flux linkage**

The stator flux linkage  $\Phi_s$  in stationary reference frame is:

$$\Phi_s = \int (V_s - R_s i_s) dt \quad (7)$$

where  $V_s$  and  $i_s$  are the stator voltage and the stator current respectively. To select the voltage vectors for controlling the amplitude of the stator flux linkage, the voltage vector plane is divided into six regions. In each region, two adjacent voltage vectors, which give minimum switching frequency, are selected to increase or decrease the amplitude of stator flux [11].

**C- Control of the rotation of stator flux linkage**

In case of PMSM,  $\Phi_s$  is changed even when zero voltage vectors are applied since the magnets rotate with the rotor. Therefore, zero voltage vectors are not used for controlling  $\Phi_s$  in PMSM. The electromagnetic torque can be controlled by controlling the amplitude and rotational speed of  $\Phi_s$ .

For counter clockwise operation, if the actual torque is smaller than the reference then the voltage vectors that keep  $\Phi_s$  rotating in the same direction are selected. If the actual torque is greater than the reference, the voltage vectors that keep  $\Phi_s$  in the reverse direction are selected instead of zero voltage vectors. By selecting the voltage vectors in this way,  $\Phi_s$  is rotated all the time and its rotational direction is determined by the output of the hysteresis controller for torque. The switching table for controlling both the amplitude and rotating direction of  $\Phi_s$  is as follows.

In Table I,  $E_\Phi$  and  $E_T$  are the output of the hysteresis controller for flux linkage and torque, respectively. If  $E_\Phi=1$  then the actual flux linkage is smaller than the reference value. The same is true for the torque. N(1, 2, ..., 6) represents the sector numbers for stator flux linkage [12].

TABLE I

$E_T$	$E_\Phi$	N					
		1	2	3	4	5	6
1	1 0	$V_2$ $V_6$	$V_3$ $V_1$	$V_4$ $V_2$	$V_5$ $V_3$	$V_6$ $V_4$	$V_1$ $V_5$
0	1 0	$V_3$ $V_5$	$V_4$ $V_6$	$V_5$ $V_1$	$V_6$ $V_2$	$V_1$ $V_3$	$V_2$ $V_4$

**IV. IMPLEMENTATION OF DTC OF PMSM**

**A- Flux linkage estimator**

As shown in the block diagram of DTC of PMSM in Fig.(2), the inverter switching states are determined according to the error of torque ( $E_T$ ) and the error of flux ( $E_\Phi$ ) [13].

$$E_T = T_{\text{eref}} - T_e \quad (8)$$

$$E_\Phi = \Phi_{\text{eref}} - \Phi_s \quad (9)$$

The stator flux linkage can be determined as follows:

$$\Phi_s = \sqrt{\Phi_\alpha^2 + \Phi_\beta^2} \quad (10)$$

$$\Phi_\alpha = \int (U_\alpha - R_s i_\alpha) dt \quad (11)$$

$$\Phi_\beta = \int (U_\beta - R_s i_\beta) dt \quad (12)$$

where  $\Phi_\alpha$  and  $\Phi_\beta$  are  $\alpha$ - $\beta$  axis fluxes,  $i_\alpha$  and  $i_\beta$  are  $\alpha$ - $\beta$  axis currents.

The  $\alpha$ - $\beta$  axis voltages ( $U_\alpha$  and  $U_\beta$ ) are calculated from the dc-link voltage  $V_{dc}$  and switching signal  $S_a, S_b$  and  $S_c$  as follows:

$$U_\alpha = \sqrt{\frac{2}{3}} V_{dc} (S_a - \frac{1}{2}(S_b + S_c)) \quad (13)$$

$$U_\beta = \sqrt{\frac{1}{2}} V_{dc} (S_b - S_c) \quad (14)$$

Also

$$i_\alpha = \sqrt{\frac{3}{2}} I_a \quad (15)$$

$$i_\beta = \sqrt{\frac{1}{2}} (I_b - I_c) \quad (16)$$

**B -Torque estimator**

The torque can be calculated from the  $\alpha$ - $\beta$  axis voltages and currents as [14]:

$$T_e = \frac{3}{2} p (\Phi_\alpha i_\beta - \Phi_\beta i_\alpha) \quad (17)$$

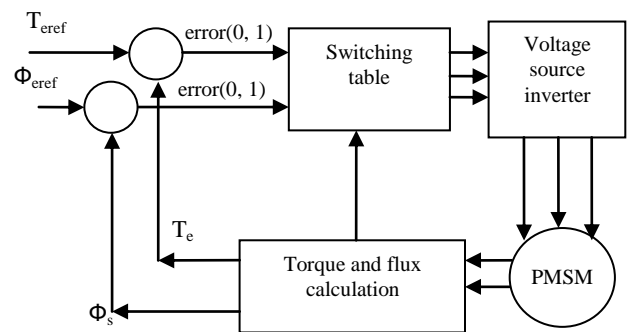


Fig. 2. Block diagram of DTC.

**V. SIMULATION RESULTS**

The simulink model of the proposed DTC of PMSM is shown in Fig.(3) under the PI speed controller. The parameters of PMSM and control parameters are shown in Table II and III, respectively (see appendix).

The simulink model implemented in this paper shown in Fig.(3) consists of seven blocks as follows:-

**A. abc-dq Conversion Block**

To convert 3-phase voltage to voltages in the 2-phase synchronously rotating frame, they are first converted to 2-phase stationary frame ( $\alpha, \beta$ ) and then from the stationary frame to the synchronously ( $dq$ ) rotating frame. The transformation is given by the following equations:

$$\begin{bmatrix} V_\alpha \\ V_\beta \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -1 & -1 \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} \quad (18)$$

$$\begin{bmatrix} V_d \\ V_q \end{bmatrix} = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix} \begin{bmatrix} V_\alpha \\ V_\beta \end{bmatrix} \quad (19)$$

**B. Motor dq-Model Block**

The dq-model of PMSM is represented according to the Eqns (1-4).

**C. dq-abc Conversion**

This conversion does the opposite of the abc-dq conversion for the current variables.

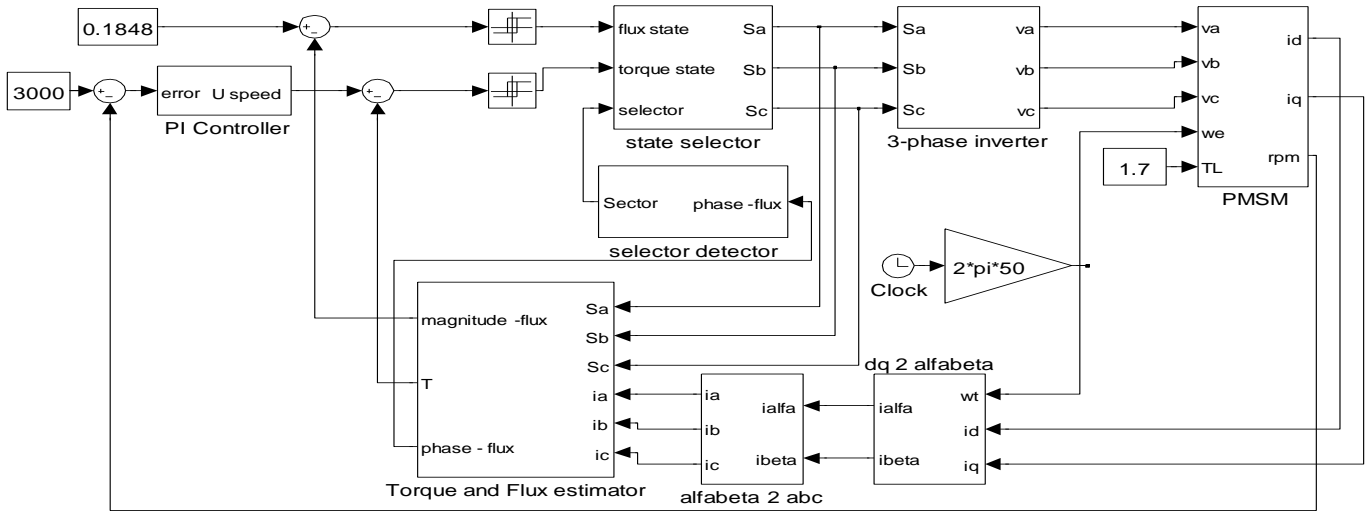


Fig. 3. DTC simulation model of PMSM.

**D. Torque and Flux Estimator Block**

This block is used to estimates the stator flux which is given in Eq.(7). This block is also used to obtain the developed electromagnetic torque produced by simulated machine using Eq.(17).

**E. Sector Detector Block**

This block is used to detect the sector of the stator flux.

**F. State Selector Block**

After the sector of stator flux, error of stator flux, and error of torque are obtained. These values are fed to direct torque control block which contains the lookup table which is used to obtain the desired voltage state vector according to the desired sectors mentioned in Table I.

**J. Three Phase Inverter Block**

This block contains two-level three-phase voltage source inverter which are controlled by the proper signal generated by the state selector block.

The steady state and dynamic performances of this model are illustrated in Figs.(4) and (5).

Fig.(4) shows the simulated dynamic performance of the torque control loop of DTC system, which is obtained by applying a step torque command from full load (1.7 N.m.) to 1 N.m. The simulated result shows that the torque ripples under DTC scheme are much smaller than those of the open loop. Also, this result confirms that the proposed DTC of PMSM is more effective method for accurate control of the electromagnetic torque.

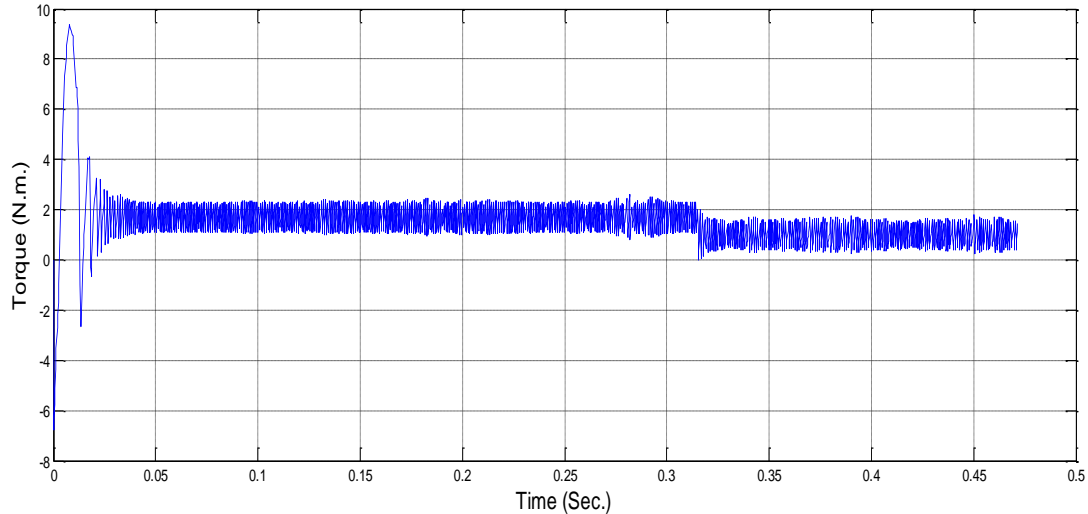


Fig. 4. Torque response with load change from full load (1.7 N.m.) to 1 N.m.

Fig.(5) shows that the estimated speed could accurately track the change of the real speed when speed reference has changed and have fast response. The proposed DTC system is relatively robust with respect to the change of speed reference

where a step speed command of 3000-2000 rpm is applied. The parameters of speed loop PI controller in this system are carefully tuned such that the optimal performance is achieved.

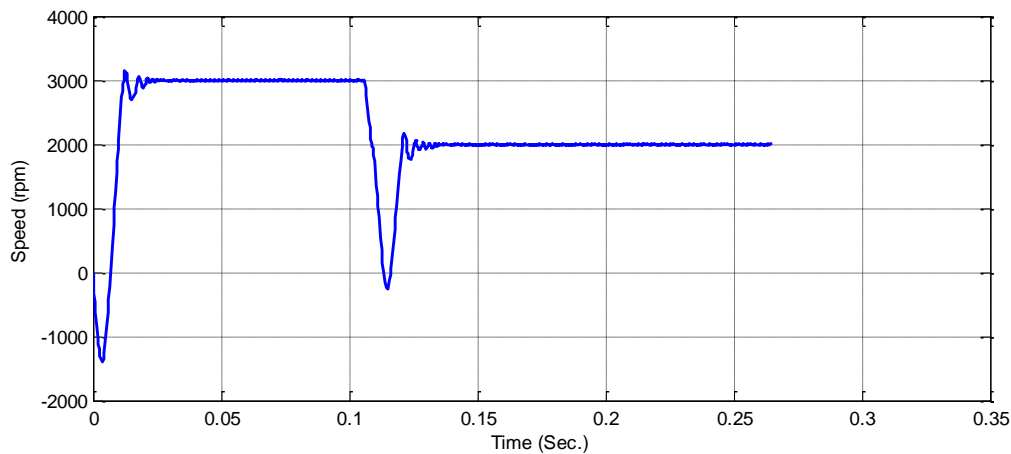


Fig. 5. Speed response with a step speed command of 3000-2000 rpm.

## VI. CONCLUSION

In this paper, Direct Torque Control with permanent magnet synchronous motor are proposed and simulated in Matlab/Simulink. This technique is used for generating a desired value of pluses by using an appropriate value of switching frequencies. The analysis carried out in this paper is aimed to propose DTC scheme in order to improve the performance of PMSM drive in terms of simple speed controller structure, fast response and torque and current low ripple. The simulation results provide the feasibility and validity of the proposed control system.

## APPENDIX A

TABLE II

Motor constants	Values
Stator resistance $R_s$	4.765 $\Omega$
Torque $T_L$	1.7 Nm
d-axis inductance $L_d$	0.014 H
q-axis inductance $L_q$	0.014 H
PM flux $\Phi_f$	0.1848 Wb
Rated speed $w$	3000 rpm
Rated current $i_s$	6.89 A
Number of poles $P$	2
Moment of inertia $J$	0.0001051
Friction factor $D$	4.047e <sup>-5</sup>
Stator flux reference $\Phi_s$	0.1848 Wb
Frequency $f$	50 Hz

TABLE III

Controller constants	Values
Integral gain $K_i$	0.089
Proportional gain $K_p$	100

## NOMENCLATURE

$f$  supply frequency

$i_d, V_d$  stator d-axis current and voltage

$i_q, V_q$  stator q-axis current and voltage

$J$  inertia of motor

$P$  pole number

$R_s$  stator phase resistance

$T_e$  electrical torque

$T_L$  load torque

$\Phi_s$  stator flux

$\Phi_f$  permanent magnet flux

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